



Seminario

Stefano Bilotta

TensorFlow and Rstudio for

Traffic Flow Reconstruction

all'interno del Corso di Big Data Architectures (prof. Paolo Nesi)





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An introduction to R

- R can be regarded as an implementation of the S language which was developed at Bell Laboratories by Rick Becker, John Chambers and Allan Wilks, and also forms the basis of the S-Plus systems (commercial licence).
- R is available as Free Software under the terms of the <u>Free Software Foundation</u>'s <u>GNU General Public License</u> in source code form. It compiles and runs on a wide variety of UNIX platforms and similar systems (including FreeBSD and Linux), Windows and MacOS.



An introduction to R

R is an integrated suite of software facilities for data manipulation, calculation and graphical display. Among other things it has:

- an effective data handling and storage facility
- a suite of operators for calculations on arrays, in particular matrices
- a large, coherent, integrated collection of intermediate tools for data analysis,
- graphical facilities for data analysis and display either directly at the computer or on hardcopy
- simple and effective programming language which includes conditionals, loops, user defined recursive functions and input and output facilities.





An introduction to R

- Free software environment
- Mathematical function and graphic module embedded
- R is functional programming language
- R is an interpreted language
- R is object oriented language

http://cran.r-project.org/src/base/





An introduction to R: packages

- R is very much a vehicle for newly developing methods of interactive data analysis. It has developed rapidly, and has been extended by a large collection of packages.
- However, most programs written in R are essentially ephemeral, written for a single piece of data analysis.
- All R functions and datasets are stored in packages. Only when a package is loaded, then its contents is available. This is done for efficiency (the full list would take more memory).
- The process of developing packages is described by formalized procedure.





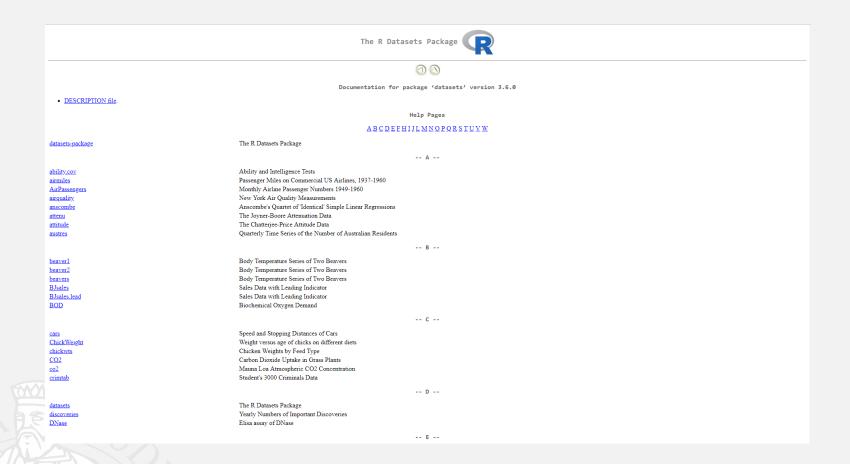
An introduction to R: packages

- The standard (or base) packages are considered part of the R source code. They contain the basic functions that allow R to work, and the datasets and standard statistical and graphical functions. They should be automatically available in any R installation.
- There exist a lot of dedicated packages regarding, for example,
 Data Import/Export, Data Mining, Linear and non-linear
 modelling, Time-Series Analysis, Classification models, Clustering
 procedures, Machine Learning, etc.





An introduction to R: R Datasets Package

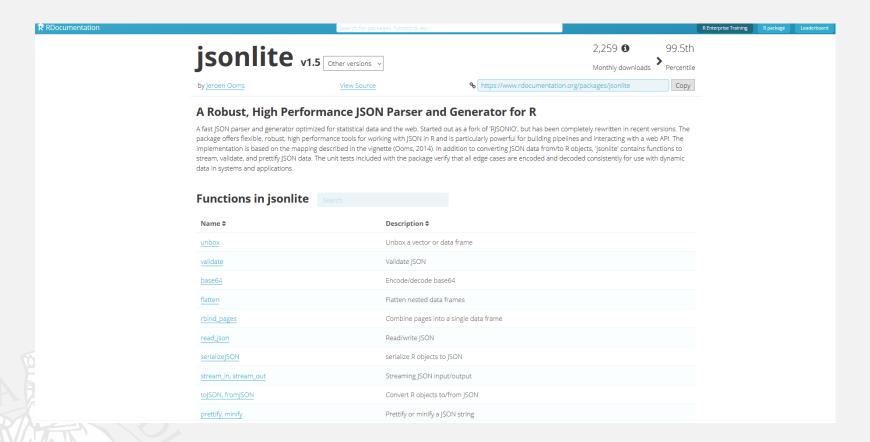






An introduction to R: packages

All packages have rich documentation:





An introduction to R: packages

All packages have rich documentation:

The jsonlite Package: A Practical and Consistent Mapping Between JSON Data and R Objects

> Jeroen Ooms UCLA Department of Statistics

Abstract

A naive realization of JSON data in R maps JSON arrays to an unnamed list, and JSON objects to a named list. However, in practice a list is an awkward, inefficient type to store and manipulate data. Most statistical applications work with (homogeneous) vectors, matrices or data frames. Therefore JSON packages in R typically define certain special cases of JSON structures which map to simpler R types. Currently there exist no formal guidelines, or even consensus between implementations on how R data should be represented in JSON. Furthermore, upon closer inspection, even the most basic data structures in R actually do not perfectly map to their JSON counterparts and leave some ambiguity for edge cases. These problems have resulted in different behavior between implementations and can lead to unexpected output. This paper explicitly describes a mapping between R classes and JSON data, highlights potential problems, and proposes conventions that generalize the mapping to cover all common structures. We emphasize the importance of type consistency when using JSON to exchange dynamic data, and illustrate using examples and anecdotes. The jsonlite R package is used throughout the paper as a reference implementation.

1 Introduction

JavaScript Object Notation (JSON) is a text format for the serialization of structured data (Crockford, 2006a). It is derived from the object literals of JavaScript, as defined in the ECMAScript Programming Language Standard, Third Edition (ECMA, 1999). Design of JSON is simple and concise in comparison with other text based formats, and it was originally proposed by Douglas Crockford as a "fat-free alternative to XML"





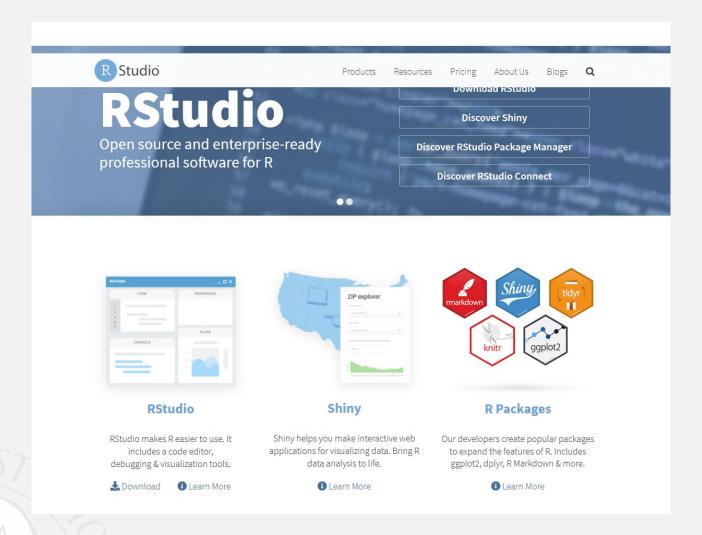
An introduction to R: Rstudio

- The most convenient way to use R is at a graphics workstation running a windowing system
- Rstudio: Take control of your code
- RStudio is an integrated development environment (IDE) for R. It includes a console, syntax-highlighting editor that supports direct code execution, as well as tools for plotting, history, debugging and workspace management.
- RStudio is available in open source and commercial editions and runs on the desktop (Windows, Mac, and Linux) or in a browser connected to RStudio Server or RStudio Server Pro (Debian/Ubuntu, RedHat/CentOS, and SUSE Linux).





An introduction to R: Rstudio







Rstudio Desktop

RStudio Desktop

	Open Source Edition	Commercial License
Overview	 Access RStudio locally Syntax highlighting, code completion, and smart indentation Execute R code directly from the source editor Quickly jump to function definitions Easily manage multiple working directories using projects Integrated R help and documentation Interactive debugger to diagnose and fix errors quickly Extensive package development tools 	All of the features of open source; plus: • A commercial license for organizations not able to use AGPL software • Access to priority support
Support	Community forums only	 Priority Email Support 8 hour response during business hours (ET)
License	AGPL v3	RStudio License Agreement
Pricing	Free	\$995/year





Rstudio Server

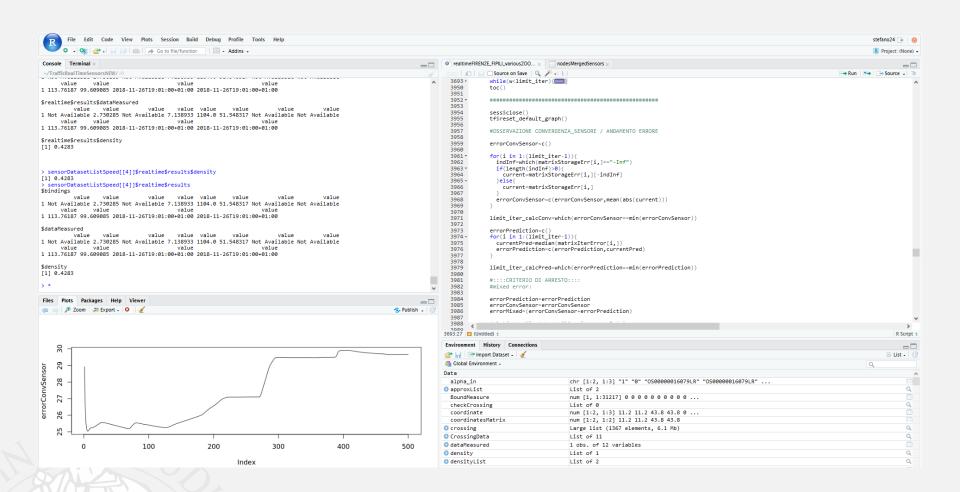
RStudio Server

	Open Source Edition	Commercial License
Overview	 Access via a web browser Move computation closer to the data Scale compute and RAM centrally 	 All of the features of open source; plus: Administrative Tools Enhanced Security and Authentication Metrics and Monitoring Advanced Resource Management
Documentation	Getting Started with RStudio Server	RStudio Server Professional Admin Guide
Support	Community forums only	Priority Email Support8 hour response during business hours (ET)
License	AGPL v3	RStudio License Agreement
Pricing	Pricing Free \$9,995/server/year Academic and Sn Business discounts available	
	DOWNLOAD SERVER	DOWNLOAD FREE RSTUDIO PRO EVAL
		📜 Purchase 🔩 Contact Sales 🖠 Info





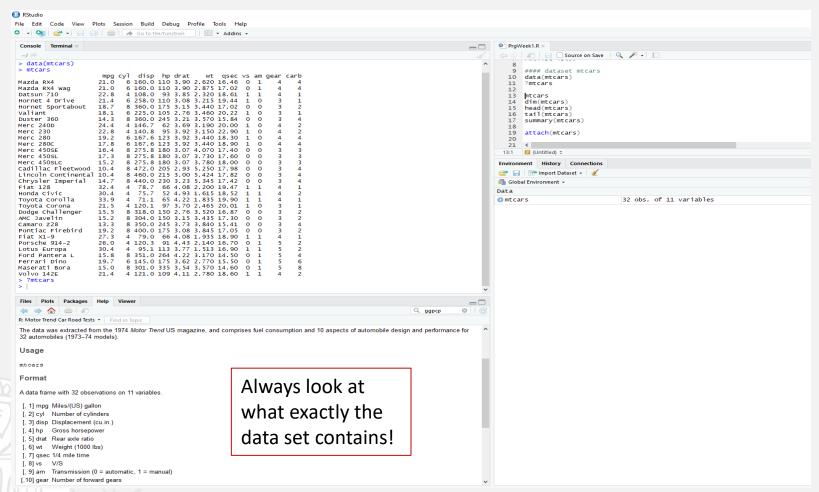
Rstudio: graphical interface







> mtcars: popular data set for examples







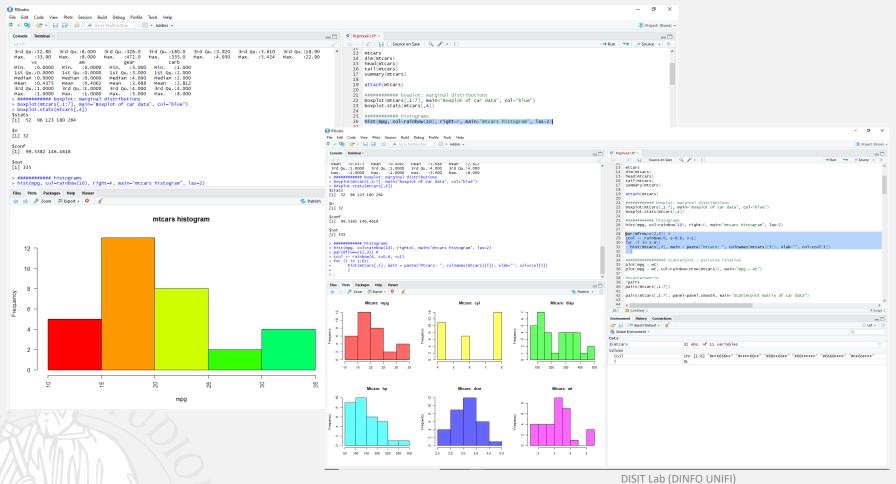
> First look at the data : Summarizing statistics

```
> summary(mtcars)
                       cy1
                                        disp
                                                           hp
                                                                           drat
      mpg
Min.
        :10.40
                  Min.
                         :4.000
                                   Min.
                                           : 71.1
                                                    Min.
                                                            : 52.0
                                                                     Min.
                                                                             :2.760
1st Qu.:15.43
                  1st Qu.:4.000
                                   1st Qu.:120.8
                                                    1st Qu.: 96.5
                                                                     1st Qu.:3.080
Median :19.20
                  Median :6.000
                                   Median :196.3
                                                    Median:123.0
                                                                     Median :3.695
        :20.09
                         :6.188
Mean
                  Mean
                                   Mean
                                           :230.7
                                                    Mean
                                                            :146.7
                                                                     Mean
                                                                             :3.597
 3rd Qu.:22.80
                  3rd Ou.:8.000
                                   3rd Qu.:326.0
                                                    3rd Qu.:180.0
                                                                     3rd Ou.:3.920
                         :8.000
                                           :472.0
                                                            :335.0
        :33.90
                                                                             :4.930
Max.
                  Max.
                                   Max.
                                                    Max.
                                                                     Max.
       wt
                       gsec
                                         VS
                                                            am
Min.
        :1.513
                  Min.
                         :14.50
                                   Min.
                                                     Min.
                                                             :0.0000
                                           :0.0000
1st Ou.:2.581
                  1st Ou.:16.89
                                   1st Ou.:0.0000
                                                     1st Ou.: 0.0000
Median :3.325
                                   Median :0.0000
                                                     Median :0.0000
                  Median :17.71
        :3.217
                         :17.85
Mean
                  Mean
                                   Mean
                                           :0.4375
                                                     Mean
                                                             :0.4062
 3rd Ou.:3.610
                  3rd Ou.:18.90
                                   3rd Qu.:1.0000
                                                     3rd Qu.:1.0000
        :5.424
                         :22.90
                                           :1.0000
                                                             :1.0000
Max.
                  Max.
                                   Max.
                                                     Max.
      gear
                       carb
Min.
        :3,000
                  Min.
                         :1.000
1st Qu.:3.000
                  1st Qu.:2.000
Median :4.000
                  Median :2.000
        :3.688
Mean
                  Mean
                         :2.812
 3rd Qu.:4.000
                  3rd Qu.:4.000
        :5.000
                         :8.000
Max.
                  Max.
```





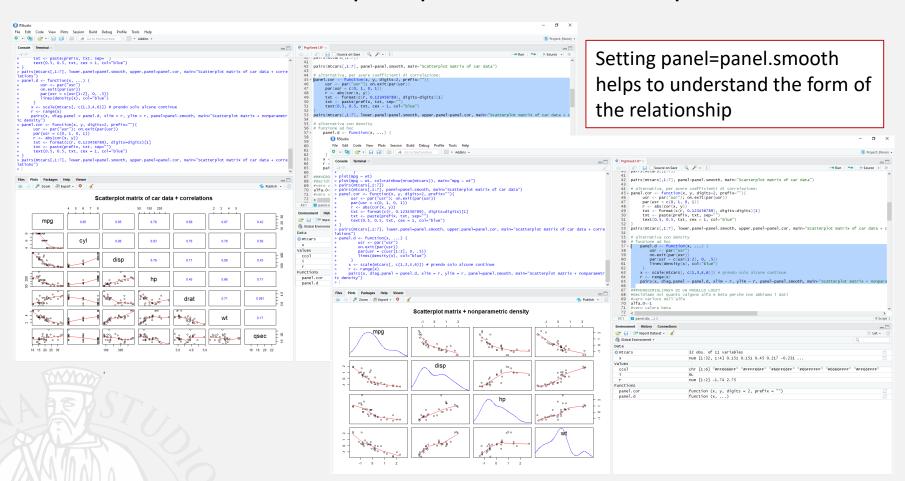
Histograms







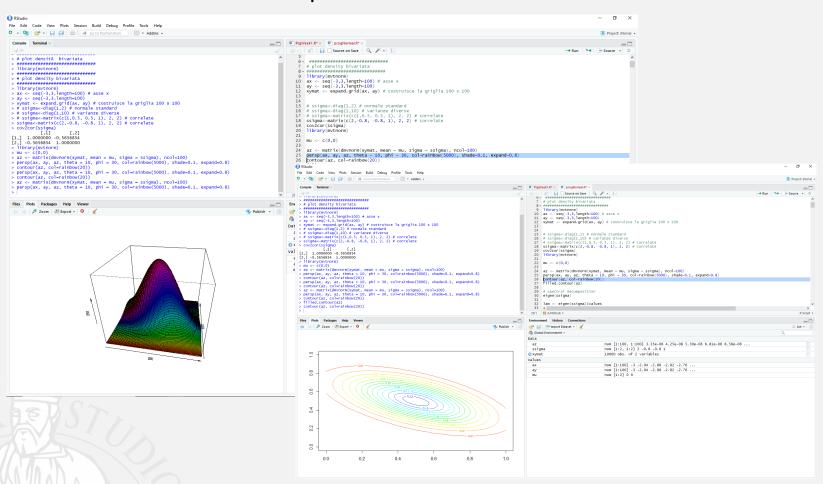
>Scatterplot: pairwise relationships







Perspective Plot and Contour Plot







An introduction to R: List

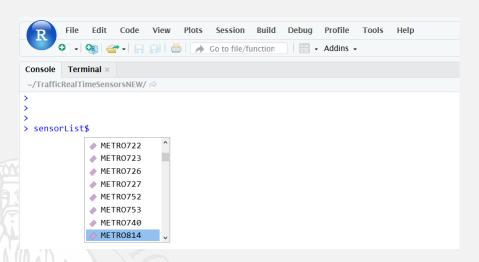
- An R list is an object consisting of an ordered collection of objects known as its components.
- There is no particular need for the components to be of the same mode or type, and, for example, a list could consist of a numeric vector, a logical value, a matrix, a complex vector, a character array, a function, and so on.
- Components are always numbered and may always be referred to as such.





An introduction to R: List

- Components of lists may also be named, and in this case the component may be referred to either by giving the component name as a character string in place of the number in double square brackets, or, more conveniently, by giving an expression of the form
 - > name\$component_name





reticulate: R interface to Python

JJ Allaire

2018-03-26

Categories: Packages R Markdown Tags: Packages R Markdown Python reticulate

We are pleased to announce the **reticulate** package, a comprehensive set of tools for interoperability between Python and R. The package includes facilities for:

- Calling Python from R in a variety of ways including R Markdown, sourcing Python scripts, importing Python modules, and using Python interactively within an R session.
- Translation between R and Python objects (for example, between R and Pandas data frames, or between R matrices and NumPy arrays).



Flexible binding to different versions of Python including virtual environments and Conda environments.



rJava - Low-level R to Java interface

REorge ne

rJava

About rJava GIT access Download/Files News Check results Package R docs

What is rJava?

rJava is a simple R-to-Java interface. It is comparable to the .c/.call C interface. rJava provides a low-level bridge between R and Java (via JNI). It allows to create objects, call methods and access fields of Java objects from R.

rJava release versions can be obtained from CRAN - usually install.packages ("rJava") in R will do the trick. The current development version can be downloaded from the files section

In a sense the inverse of rJava is JRI (Java/R Interface) which provides the opposite direction - calling R from Java. JRI is now shipped as a part of the rJava package, although it still can be used as a separate entity (especially for development). Currently rJava is used as a part of JGR, iPlots and JavaGD software/packages.

About rJava

Please report any bugs or wishes related to rJava or JRI using Issues on GitHub.

What's new?

rJava source repository is now on GitHub and that is also the place to report bugs. The main page and builds are still on RForge.net.

2016/01/06 - rJava 0.9-8 released. Mostly work-arounds for bugs in Oracle Java on OS X - see NEWS for details.

2015/07/27 - rJava 0.9-7 released. Mostly various bugfixes - see NEWS for details.

2012/12/23 - rJava 0.9-6 released. Fixes Java parameter issue introduced in 0.9-5 on systems with headless mode (e.g. OS X).

2011/06/22 - rJava 0.9-0 released. This is a major upgrade that changes behavior of array references in low-level calls back to early 0.8 state as intedended by the original design. It should be more consistent now. We have had rJava 0.9-0 in RC state for a long time so hopefully all developers relying on rJava have checked their packages. For the full list of fixes and changes see NEWS.

2009/10/27 - rJava 0.8-0 released. Many new features mostly thanks to Romain Francois -- check the NEWS file for details.

2009/08/22 - rJava 0.7-0 released. Recommended update (includes bugfixes to fields handling, new support for with(), method/field auto-completion and more forgiving \$ operator), includes JRI 0.5-0.

2008/09/22 - rJava 0.6-0 released. Adds support for Java serialization and R-side cache which enables Java objects to become persistent across sessions. See ? . jcache in R (or the online help) for details.

2007/11/05 - rJava 0.5-1 released. Fixes issues with Windows; and minor updates (see NEWS).

2007/08/22 - rJava 0.5-0 released. This is a major update featuring many new features and bugfixes. It sports a new custom class loader, much improved (and faster) field support, integration of all native Java types, automatic fall-back to static methods, infrastructure for writing Java packages easily (see .jpackage), support for custom convertors and call-backs. Please read the NEWS file for details.

2007/02/27 - rJava 0.4-14 (update is recommended to all users due to memory leak fixes), please use CRAN to get the latest release. The current development version is rJava 0.5-0 (available from here - see SVN access and download on the left). It is under heavy construction right now with many new features, so feel free to test-drive it if you want to be on the bleeding edge (it is a bit chatty as some debugging output is still enabled). Some of the highlights are memory profiler, intelligent class loader, easy Java package interpration and callback support.





Advanced R by Hadley Wickham

Table of contents -

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Calling C functions from R
C data structures
Creating and modifying vectors
Pairlists
Input validation
Finding the C source code for a function

How to contribute

Edit this page

R's C interface

Reading R's source code is an extremely powerful technique for improving your programming skills. However, many base R functions, and many functions in older packages, are written in C. It's useful to be able to figure out how those functions work, so this chapter will introduce you to R's C API. You'll need some basic C knowledge, which you can get from a standard C text (e.g., The C Programming Language by Kernigan and Ritchie), or from Rcpp. You'll need a little patience, but it is possible to read R's C source code, and you will learn a lot doing it.

The contents of this chapter draw heavily from Section 5 ("System and foreign language interfaces") of Writing R extensions, but focus on best practices and modern tools. This means it does not cover the old .C interface, the old API defined in Rdefines.h, or rarely used language features. To see R's complete C API, look at the header file Rinternals.h. It's easiest to find and display this file from within R:

rinternals <- file.path(R.home("include"), "Rinternals.h")
file.show(rinternals)</pre>

All functions are defined with either the prefix Rf_ or R_ but are exported without it (unless #define R_NO_REMAP has been used).

I do not recommend using C for writing new high-performance code. Instead write C++ with Rcpp. The Rcpp API protects you from many of the historical idiosyncracies of the R API, takes care of memory management for you, and provides many useful helper methods.

Outline

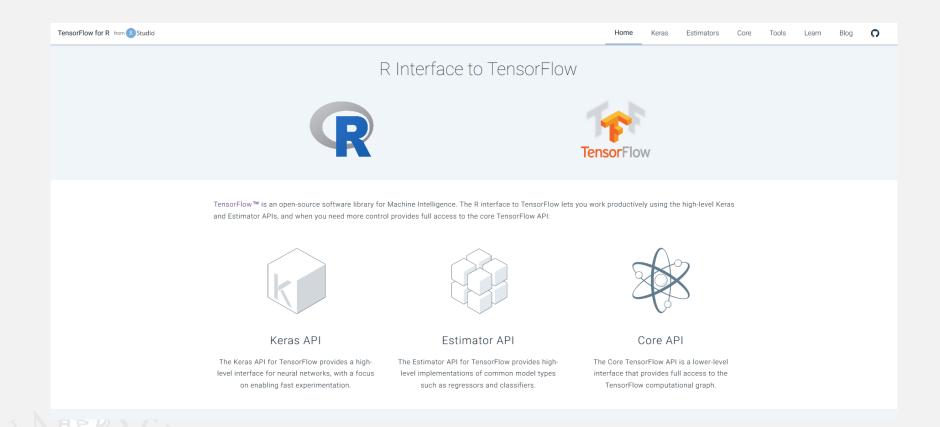
- . Calling C shows the basics of creating and calling C functions with the inline package.
- . C data structures shows how to translate data structure names from R to C.
- . Creating and modifying vectors teaches you how to create, modify, and coerce vectors in C.
- Pairlists shows you how to work with pairlists. You need to know this because the distinction between pairlists and list is more important in C than R.
- . Input validation talks about the importance of input validation so that your C function doesn't crash R.
- Finding the C source for a function concludes the chapter by showing you how to find the C source code for internal and primitive R functions.

Prerequisites

To understand existing C code, it's useful to generate simple examples of your own that you can experiment with. To that end, all examples in this chapter use the inline package, which makes it extremely easy to compile and link C code to your current R session. Get it by running install.packages("inline"). To easily find the C code associated with internal and primitive functions, you'll need a function from pryr. Get the package with install.packages("pryr").











An introduction to TensorFlow

- TensorFlow is an open source software library for numerical computation using data flow graphs.
- Nodes in the graph represent mathematical operations, while the graph edges represent the multidimensional data arrays (tensors) communicated between them.
- The flexible architecture allows you to deploy computation to one or more CPUs or GPUs in a desktop, server, or mobile device with a single API.





An introduction to TensorFlow

- TensorFlow was originally developed by researchers and engineers working on the Google Brain Team within Google's Machine Intelligence research organization for the purposes of conducting machine learning and deep neural networks research, but the system is general enough to be applicable in a wide variety of other domains as well.
- Tensorflow is one of the widely used libraries for implementing algorithms involving large number of mathematical operations.
- A detailed guide can be found in www.tensorflow.org/guide





DataFlow Graph

- TensorFlow uses a dataflow graph to represent your computation in terms of the dependencies between individual operations.
 Then it is necessary to create a TensorFlow session to run parts of the graph across a set of local and remote devices.
- DataFlow is a common programming model for parallel computing. In a dataflow graph, the nodes represent units of computation, and the edges represent the data consumed or produced by a computation.





DataFlow Graph

- Dataflow has several advantages that TensorFlow leverages when executing your programs:
 - Parallelism. By using explicit edges to represent dependencies between operations, it is easy for the system to identify operations that can execute in parallel.
 - Distributed execution. By using explicit edges to represent the values that flow between operations, it is possible for TensorFlow to partition your program across multiple devices (CPUs, GPUs, and TPUs) attached to different machines. TensorFlow inserts the necessary communication and coordination between devices.



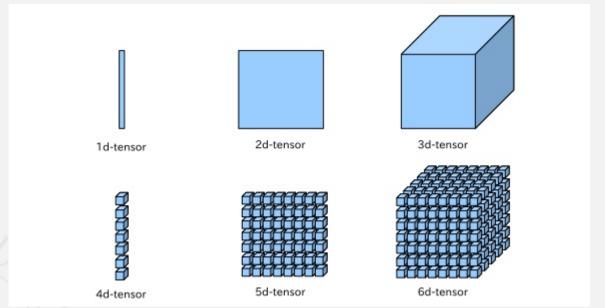
 TensorFlow, as the name indicates, is a framework to define and run computations involving tensors. A **tensor** is a generalization of vectors and matrices to potentially higher dimensions. Internally, TensorFlow represents tensors as n-dimensional arrays of base datatypes.

Rank	Math entity
0	Scalar (magnitude only)
1	Vector (magnitude and direction)
2	Matrix (table of numbers)
3	3-Tensor (cube of numbers)
n	n-Tensor (you get the idea)





In particular, Tensor is a general name of multi-way array data.
 For example, 1d-tensor is a vector, 2d-tensor is a matrix and 3d-is a cube. We can image 4d-tensor as a vector of cubes, 5d-tensor is a matrix of cubes and 6d-tensor is a cube of cubes







- When writing a TensorFlow program, the main object you manipulate and pass around is the tf.Tensor (in R . -> \$).
- A tf. Tensor has (necessarily) the following properties:
 - a data type (float32, int32, ecc.)
 - a shape
- TensorFlow programs work by first building a graph of *tf. Tensor* detailing how each tensor is computed based on the other available tensors and then by running parts of this graph to achieve the desired results.
- Then, a *tf. Tensor* object represents a partially defined computation that will eventually produce a value.



- Some types of tensors are special, the main are:
 - tf.Variable
 - tf.constant
 - tf.placeholder
- In general, with the exception of *tf.Variable*, the value of a tensor is immutable, which means that in the context of a single execution tensors only have a single value.
- Each element in the Tensor has the same data type, and the data type is always known. The shape (that is, the number of dimensions it has and the size of each dimension) might be only partially known. Most operations produce tensors of fully-known shapes if the shapes of their inputs are also fully known.





Variables

- A TensorFlow variable is the best way to manipulate your program.
- Before you can use a variable in a *session run*, it must be initialized and they have to be explicitly initialized.
- To initialize all trainable variables in one go, before training starts, call tf\$global_variables_initializer()
- Just like any other TensorFlow operation, you can place variables on particular devices (in the case of more than one Graphic Devices)





Variables

 For example in the following case it is possible to set the session run on the GPU:0 by means tf\$device('/gpu:0')

NVIDIA-SMI 375.26 Driver Version: 375.26				
GPU	Name	Persistence-M	Bus-Id Disp.A	Volatile Uncorr. ECC
Fan	Temp Perf	Pwr:Usage/Cap	Memory-Usage	
0	Graphics De	vice Off	0000:02:00.0 Off 4449MiB / 12189MiB	N/A
1	Quadro K620	Off	0000:07:00.0 Off	
38%	50C P8	1W / 30W	228MiB / 1997MiB	N/A





Session Run

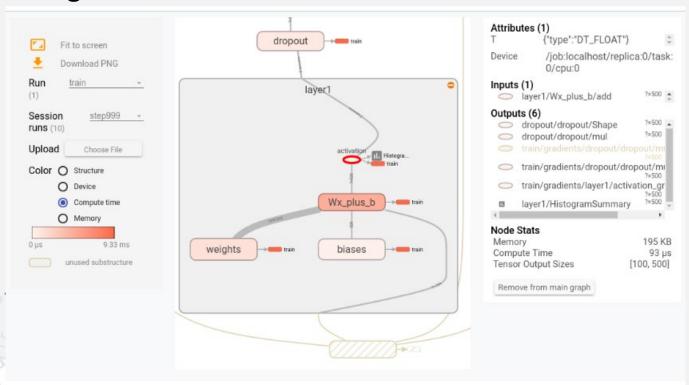
- TensorFlow uses the *tf\$Session* class to represent a connection between the client program (typically a Python program, although a similar interface is available in other languages, as R in this case) and the C++ runtime.
- A tf\$Session object provides access to devices in the local machine, and remote devices using the distributed TensorFlow runtime.
- After the runtime, a *tf\$Session* object have to be closed to free the resoures.





TensorBoard: Graph Visualization

 Often, TensorFlow computation graphs are powerful but complicated. The graph visualization can help you understand and debug them.





Welcome to the Traffic Flow Reconstruction







Overview

We aim to improve the urban mobility through a **general** and **self-adaptive** model for a **low-cost** traffic reconstruction at **real-time** in **every position** of the city.

We propose to use a **fluid-dynamic traffic model** on road networks getting the road infrastructure and traffic restrictions from the **Open Street Map** and the traffic sensors specifications and detections from the **publicly available Open Data**.



Features

Low-cost

It uses stationary sensors that were already deployed in the city.

Real-Time

The reconstruction is updated after every new traffic sensor detection.

Unobtrusive

It does not require users to take any action (install app, submit data...).

General

No simplistic assumption is made about the street graph.

Visual

Traffic flows are displayed on a street map through colored lines.

Dense

The reconstruction is made at every location in the area of interest.

Open

Methods and software are made available under an open license.

Verified

The accuracy of the reconstruction has been rigorously verified.

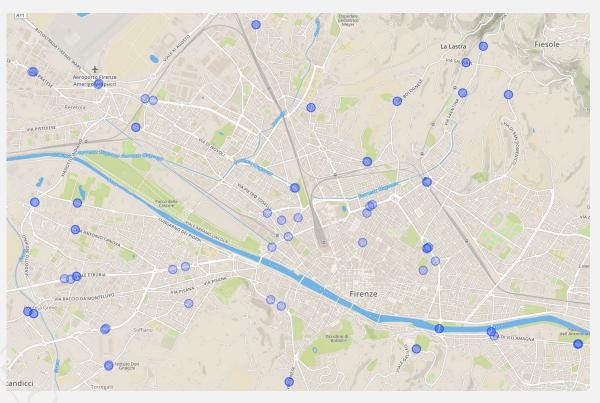






Target

• Starting from fixed traffic sensors scattered in the city, our scope is the prediction/reconstruction of the real-time vehicular traffic density in the whole urban network.







Ingestion process

- Given a generic geographic area of observation, an ingestion process is needed in the Km4city Knowledge Base to import both the detailed real street paths and the sensors data placed in the selected area
- The traffic data from stationary sensors in a municipality (spire road sensors and cameras) give the state of the traffic counting the number of vehicles which pass through the supervised area and the data are simultaneously uploaded 10 minutes.



Km4City – A Knowledge Model for Smart Cities



An Open Urban Platform for a Sentient Smart City, aimed at:

- Implementing the city vision;
- Monitoring the city evolution;
- Providing new services for improving the quality of life of the citizens;
- Supporting the economic grow of the city;
- Promoting virtuous behaviours.

Briefly, we aim to support cities that produce with happy and proud citizens and with crowds of enthusiastic tourists and investors.





Open Street map

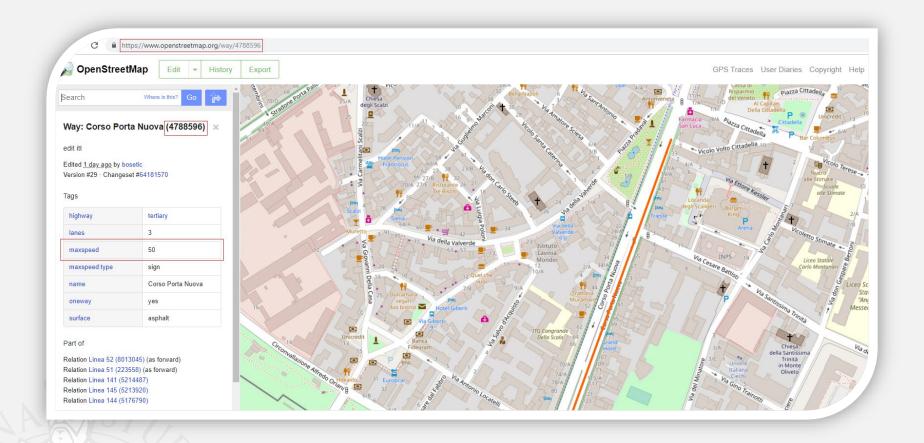


- OpenStreetMap powers map data on thousands of web sites, mobile apps, and HW devices.
- It is built by a community of mappers that contribute and maintain data about roads, trails, cafés, railway stations, and much more, all over the world.
- It provides open data: you are free to use it for any purpose as long as you credit OpenStreetMap and its contributors.
- OSM data is stored in a RDB, and then transformed and stored in a triplestore, based on a mapping of the OSM data model to the Km4City Ontology street graph modelling.





Data from OSM







Sensors and detections

- Traffic Sensors static information (identifier, geolocation, street address, technical specifications...) and the traffic flow detections (sensor, timestamp, detected traffic flow, estimated speed...) all come from publicly available Open Data.
- They are managed through ETL processes, and stored in a No-SQL database.
- The traffic reconstruction model implementation accesses those data through dedicated APIs. Traffic flows are read every 10 minutes, the refresh frequency of the traffic sensors.





Mathematical model

- The traffic sensor detections are interpreted as sources of traffic leading into the outcoming roads of the nodes where sensors are located.
- We consider a mathematical model for fluid dynamic flows on networks which is based on conservation laws.
- Road network is studied as a directed graph composed by arcs that meet at some nodes, corresponding to junctions.





Mathematical model

- We deal with the fluid-dynamic models which can be seen as a macroscopic model which allows to observe the network in the time evolution through waves formation.
- In a single road, this nonlinear model is based on the conservation of cars described by the following scalar hyperbolic conservation law (1)

$$\frac{\partial \rho(t, x)}{\partial t} + \frac{\partial f(\rho(t, x))}{\partial x} = 0$$

$$\rho(t,a) = \rho_a(t)$$
 and $\rho(t,b) = \rho_b(t)$

$$\rho(0,x) = \rho_0(x).$$





Mathematical model

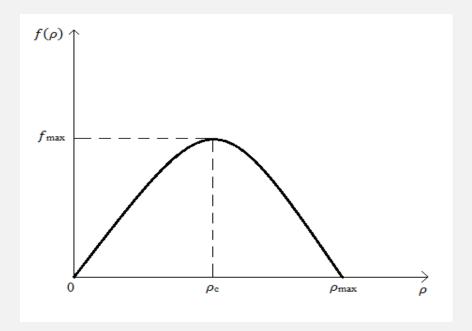
- $\rho(t,x)$ denotes the car density which admits values from 0 to $\rho_{\rm max}$, where $\rho_{\rm max}$ > 0 is the maximal vehicular density on the road.
- The function $f(\rho(t,x))$ is the vehicular flux which is defined as the product $\rho(t,x)v(t,x)$, where v(t,x) is the local speed of the cars.
- As usually it happens, in the case of first order approximation, if we assume that v(t,x) is a decreasing function, only depending on the density, then the corresponding flux is a concave function





Fundamental diagram

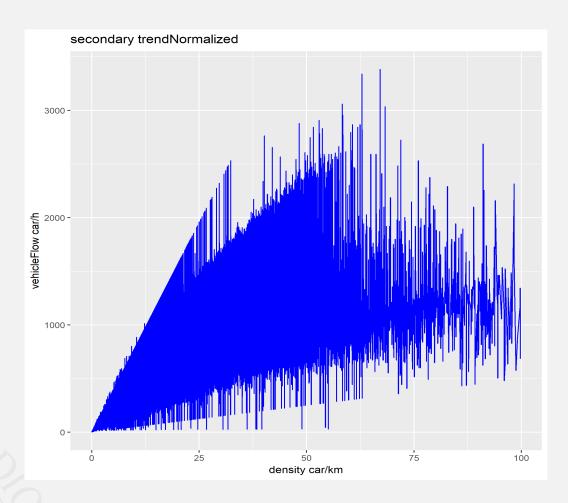
• We consider the local cars' speed as $v(\rho)=v_{max}(1-\frac{\rho}{\rho_{max}})$ obtaining that $f(\rho)=v_{max}\left(1-\frac{\rho}{\rho_{max}}\right)\rho$, where v_{max} is the limit speed







Fundamental diagram: data analysis







Discretization scheme

The following discretization and simplification of the model is operated:

- Each road is partitioned in segments Δx long.
- The time is partitioned in intervals Δt long.
- Denote (h,m) a bounded time-space region (cell) of duration h and length m. Let $u_m^h = u(t_h, x_m) = u(h\Delta t, m\Delta x)$ be a continuous function defined on (h,m). Denote F the numerical flux. Then, the vehicular density results from:

$$u_m^{h+1} = u_m^h - \frac{\Delta t}{\Delta x} \left(F(u_m^h, u_{m+1}^h) - F(u_{m-1}^h, u_m^h) \right)$$





Sensors' measurements

- The measured data sensor is interpreted as the source of traffic leading into the outcoming roads of the considered junction.
- suppose to assign a condition at the incoming boundary for x=0 as $\rho(t,0)=\rho_b^{inc}(t)$.
- we proceed by inserting an "incoming ghost cell" and the discretization becomes

$$u_0^{h+1} = u_0^h - \frac{\Delta t}{\Delta x} \left(F(u_0^h, u_1^h) - F(v_{(inc)}^h, u_0^h) \right)$$

where

$$v_{(inc)}^{h} = \frac{1}{\Delta t} \int_{t_h}^{t_h+1} \rho_b^{inc}(t) dt$$

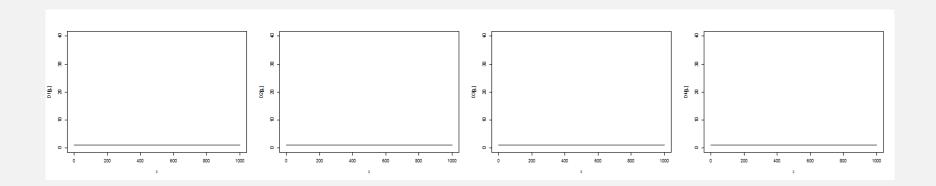
• replaces the "ghost value" u_{-1}^h





Fluid Dynamics Approach

Phisical Principle of Narrowing in roads







Numerical meaning

```
[,6]
                                                                                 [,8]
                               [,3]
                                          [,4]
                                                    [,5]
                                                                                           [,9]
                 8.938677
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       9.343250
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                 9.074992
                           8.747273
```





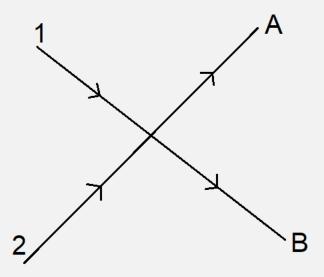
Application of the model

- For each time slot t, each traffic sensor detection is interpreted as
 a source of traffic that leads into the segments of road that origin
 from the node where the sensor is located that has produced the
 data.
- The vehicular traffic flow is propagated in the network according to the fluid dynamic model in (1).
- The distribution of the traffic at crossroads is governed by a
 Traffic Distribution Matrix whose coefficients are based on the weights of the segments of roads that make the crossroad.





Traffic distribution on a junction

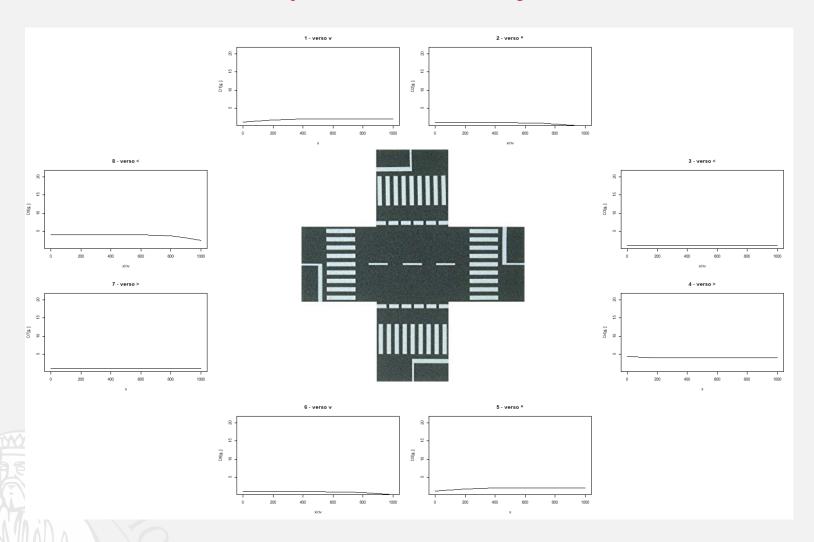


$$\begin{pmatrix} d_{1A} & d_{2A} \\ d_{1B} & d_{2B} \end{pmatrix} \begin{pmatrix} f_1 \\ f_2 \end{pmatrix} = \begin{pmatrix} f_A \\ f_B \end{pmatrix}$$





Fluid Dynamics of a junction









The fork of via Mafalda di Savoia (East), in via Mafalda di Savoia (South), Viale Giovanni Milton (West) and Via del Ponte Rosso (North), in Florence.





Road Type: primary

Lanes: 2

Designated Lanes: 0 Restrictions: none Learning Factor: 61

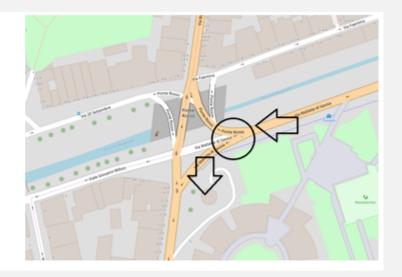
Elem. Type: T.O.C.

Length: 63

Direction: positive

•••

Weight: 31.122%







Road Type: tertiary

Lanes: 1

Designated Lanes: 0 Restrictions: none Learning Factor: 24

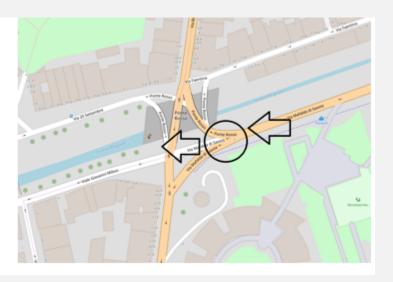
Elem. Type: T.O.C.

Length: 51

Direction: positive

•••

Weight: 12.245%







Road Type: primary

Lanes: 2

Designated Lanes: 0 Restrictions: none Learning Factor: 111

Elem. Type: T.O.C.

Length: 60

Direction: positive

•••

Weight: 56.633%







Weight initialization

Weights are initialized based on the following:

- Road type: motorway, trunk, primary, secondary, tertiary, unclassified, residential, service;
- Lanes: how many lanes are drawn on the asphalt, also considering possible restrictions (e.g. lanes reserved to public transport);
- **Traffic restrictions**: examples are mandatory/forbidden directions at crossroads, speed limits, limited traffic zones.





Stochastic learning

It has been observed that:

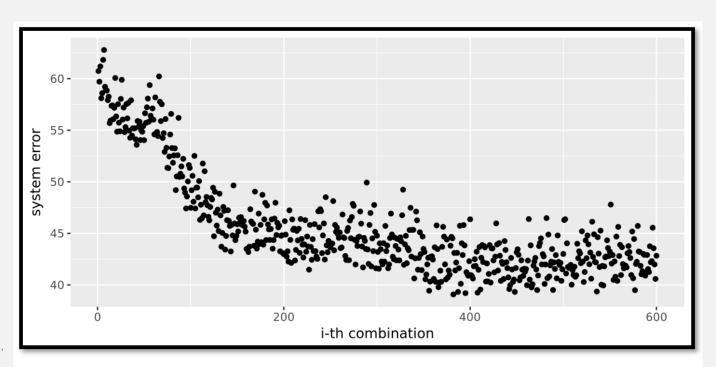
- The way how vehicles distribute at crossroads varies depending of the day of the week, and of the time of the day;
- A random variation of some weights is very likely to lead to an improved accuracy;
- If no improvements are achieved after *n* attempts, it is reasonable to move anyway to the best of the last *n* configs.

An offline process is run, based on the above, that leads to timebased weight adjustments, aimed at an improved accuracy.





Stochastic learning



In the x axis, the number of the learning iterations. In the y axis, the (decreasing) system error.





Validation approach

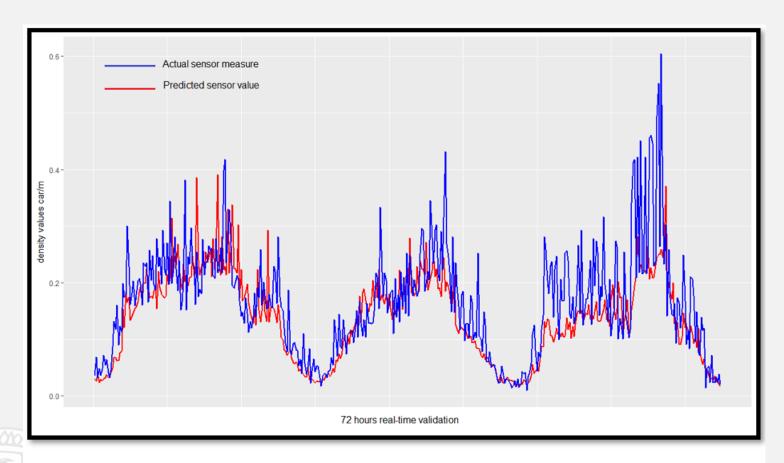
- Let the **error at a sensor at a given time** *t* be the percentage error computed removing a *given sensor* from the inputs and comparing the traffic flow *reconstructed* at the sensor with the traffic flow *detected* by the sensor, at the given time.
- Let the system error over a time period T be the average of the system errors computed over all the traffic sensors and all the times t∈ T.

The system error has been computed to be the **30%** about.





Validation approach



The diagram refers to one in particular of the sensors, and it displays the predicted vs actual values over the time in the 72 hours validation.



Displaying results

- Segments of road are categorized based on the road type and the number of lanes.
- Segments of each category that have one at least of the extremities that coincide with a traffic sensor, are used for determining the range of the traffic flows that can be observed on the specific category of segments.
- For each segment category, the range is partitioned into four subranges, that correspond to the four colors that you can find on the map.
- The reconstruction is presented to users through colored lines traced over the road paths on the city map.
- The date and time when the most up-to-date values from the sensors have been acquired can also be seen at the top-right corner of the map.



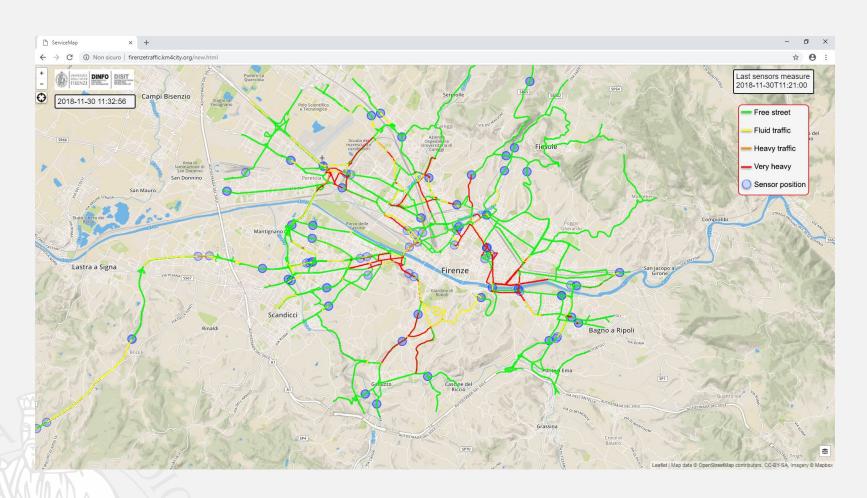
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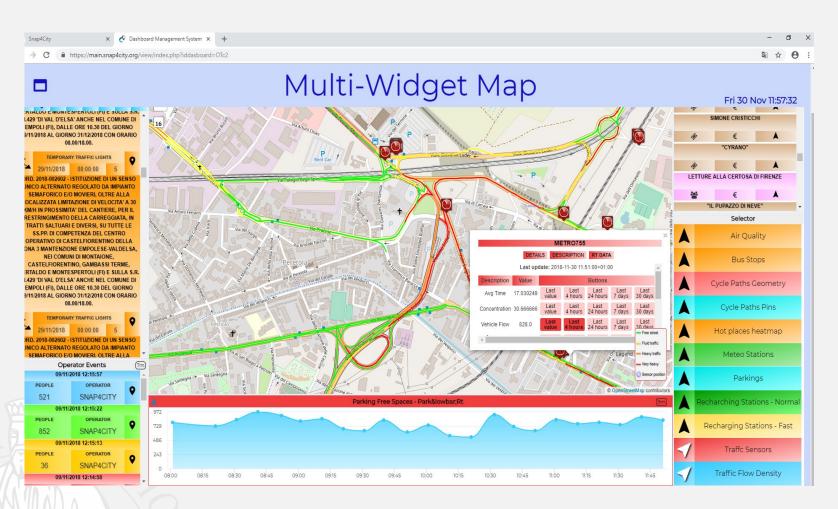
Displaying results







Displaying results: on dashboard







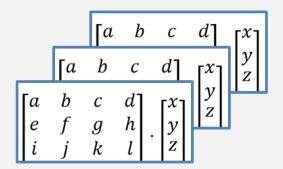
Data structure in real-time computing

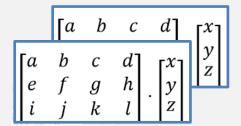
- A network area of Florence consisting of 173 data sensors (■),
 1532 junctions and 1377 road-segments giving the estimation of
 the vehicular density in 31217 road-units having length 20/30
 meters is considered to test the model
- Parallel computing of road-units by 1d-tensor (complex indexing)
- Parallel computing of junctions by 3d-tensor
- Each update of the sensors is every 10 minutes.





Graphical idea of real-time computing



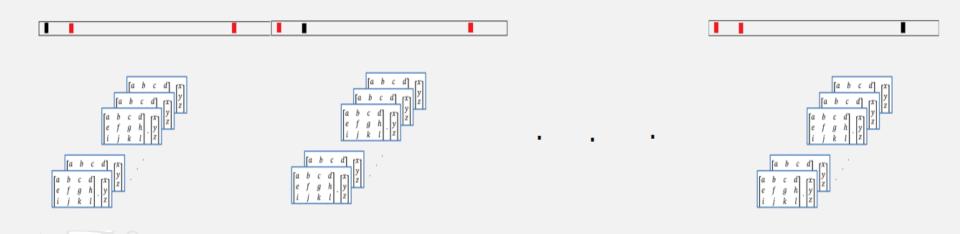






Data structure in Stochastic Learning

 The Graph structure is repeated for about 60 removed sensors obtaing a concatenated data structure having about 2000000 road-units computed in parallel.







Thanks for your attention

We gratefully acknowledge the support of NVIDIA Corporation with the donation of the Titan Xp GPU used for this research